

# A crash course in using tide gauges to study sea level

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# An outline of today's lecture

At the end of this lecture I hope you have answers to these questions

- Why do we have tide gauges and how do they work?
- Where are they located and how can I find the data?
- What signals can I expect in a tide-gauge record?
- How we can reconstruct regional and global sea-level changes from tide gauges

Feel free to ask questions!

## A quick history of tide-gauge observations, and where to get the data

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# A quick history of tide-gauge observations

Reading from a tide pole



Sources: Rijkswaterstaat Beeldbank and Phil Woodworth

Tidal tables for sailors

JANUARY, 1781.										Clock bef. Sun.
D. H. M.					D. H. M.					
First Qr.	28	1	E.	Full Moon	10	8	51M.			
Last Qr.	17	1	40M.	New Moon	24	11	58M.			
DAYS.		Morn.		Even.		Heights				
		H.	M.	H.	M.	2.	1.	M.		
Monday	1	3	3	3	24	13	0	4		
Tuesday	2	3	47	4	11	12	4	5		
Wednesday	3	4	37	5	4	11	9			
Thursday	4	5	34	6	6	11	8			
Friday	5	6	38	7	10	11	10	6		
Saturday	6	7	44	8	13	12	6			
SUNDAY	7	8	41	9	7	13	5	7		
Monday	8	9	31	9	55	14	5			
Tuesday	9	10	18	10	40	15	5	8		
Wednesday	10	11	2	11	24	16	5			
Thursday	11	11	45			17	4			
Friday	12	0	7	0	28	18	0	9		
Saturday	13	0	50	1	13	18	3			

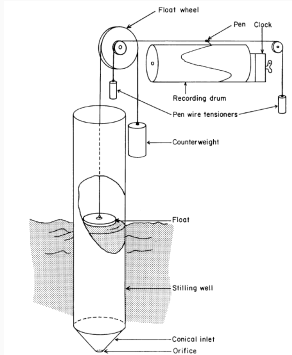
# From tidal measurements to long-term changes

Johannes Hudde, mayor of Amsterdam built benchmarks to create uniform height for flood defenses in 1675. One benchmark still exists today



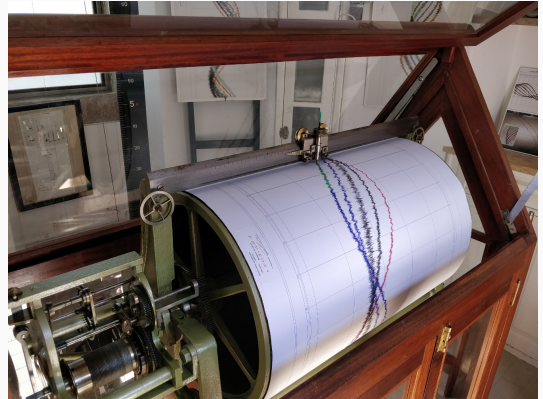
# From tidal measurements to long-term changes

## Automatic float tide gauges



Sources: Phil Woodworth, Wikipedia

## From manual recordings to paper rolls



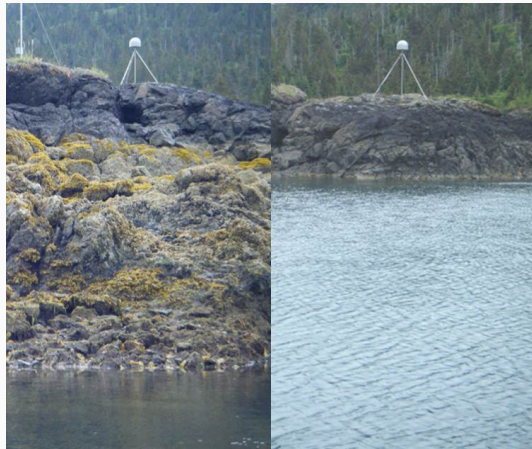
# Nowadays most tide gauges are equipped with more modern instruments

## Radar gauges



Sources: Phil Woodworth, Kristine Larson

## GPS reflectometry



# Where to find tide-gauge data?

There are multiple freely available databases with tide-gauge data.

Use the right database, depending on what you need:

- High-frequency data (10-min, hourly or daily):
  - GESLA database ([gesla.org](http://gesla.org))
  - University of Hawaii Sea Level Center ([uhslc.soest.hawaii.edu](http://uhslc.soest.hawaii.edu))
  - Real-time data: VLIZ/IOC ([www.ioc-sealevelmonitoring.org](http://www.ioc-sealevelmonitoring.org))
- Long-term changes (monthly or annual data):
  - PSMSL: Permanent Service for Mean Sea Level ([www.psmsl.org](http://www.psmsl.org))
- But there is more! Local authorities, data rescue projects etc...

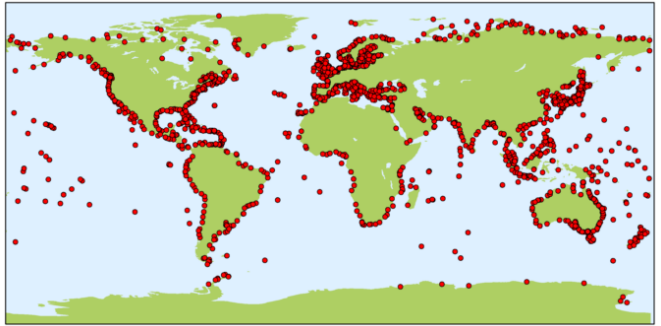


# Permanent Service for Mean Sea Level

PSMSL:

- collects
- analyses
- distributes

monthly and annual  
sea-level data



All stations for which PSMSL has data

## Long records



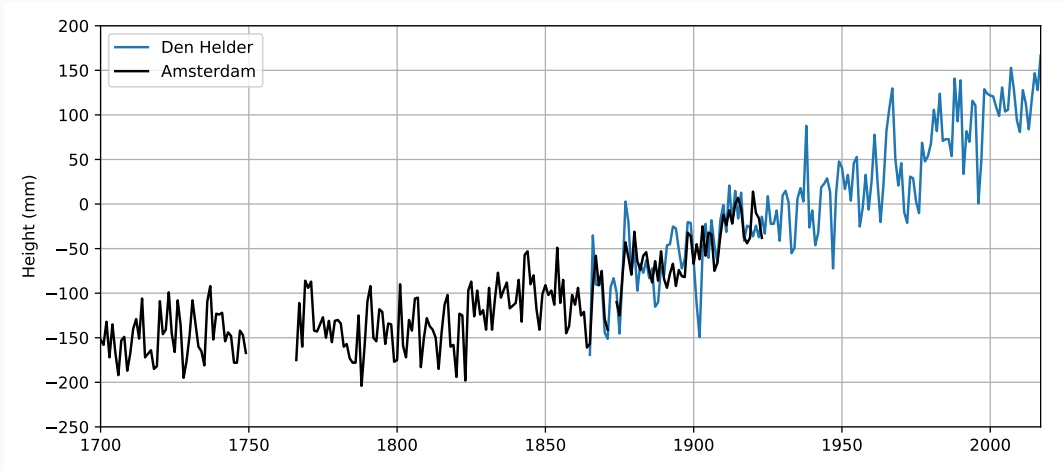
All stations with more than 40 years of data

Long records:

- Comparably few stations
- Not evenly distributed
- Southern hemisphere sparsely covered

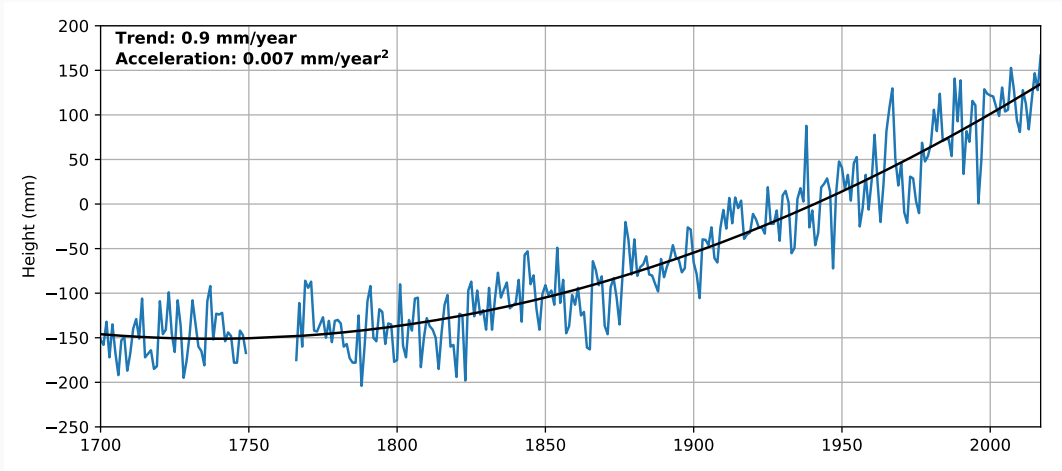
# Long records: Amsterdam

Oldest known tide-gauge record, thanks to Johannes Hudde



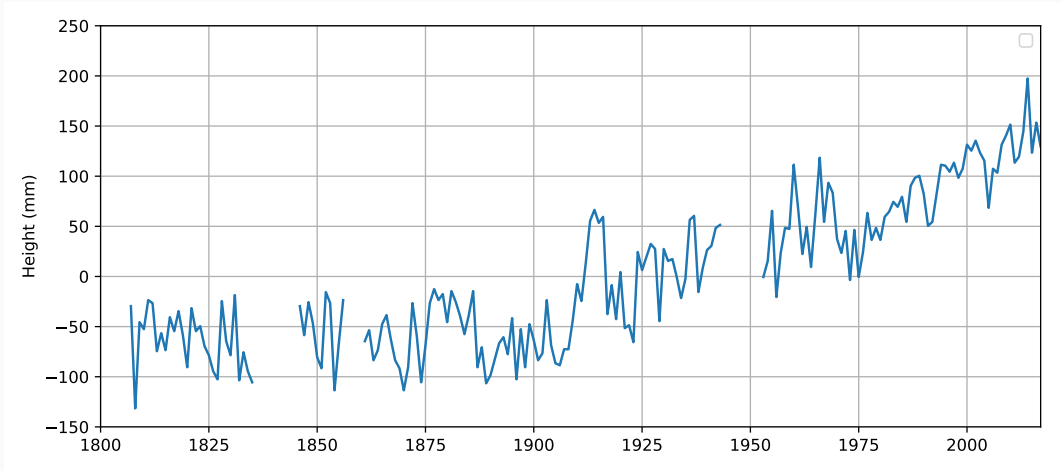
# Long records: Amsterdam

Record points at accelerating sea level:



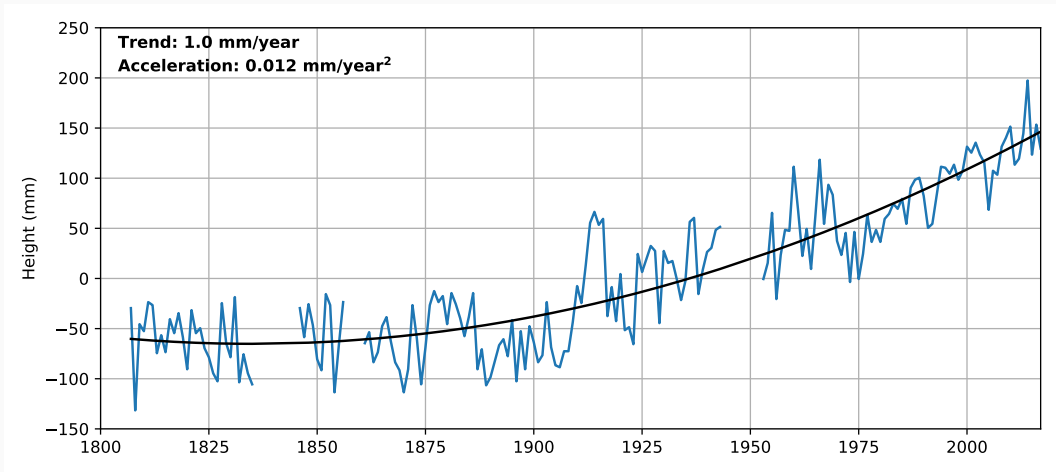
# Long records: Brest

Oldest tide-gauge locations with ongoing measurements



# Long records: Brest

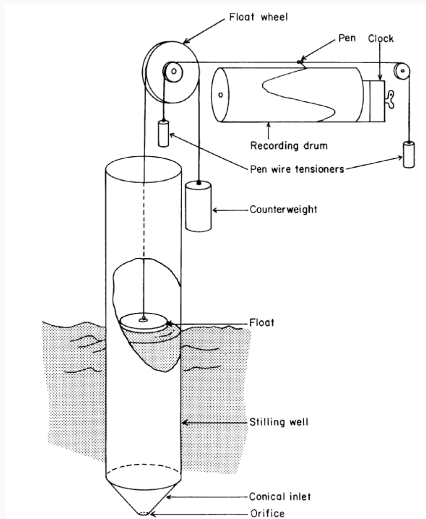
Also points at a sea-level acceleration



A few things to keep in mind when  
using tide-gauge data

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# Tide gauges often use a stilling well, which removes high-frequency signals



Tide gauges often use a stilling well. This removes a lot of noise from the measurements, but a stilling well works as a low-pass filter:

- Effects of waves and tsunamis are not recorded or distorted
- A stilling well does retain tides and surges
- Tide gauges are often in harbours and thus do not measure in the ocean directly

**Make sure that the tide gauge records the signal you're looking for!**



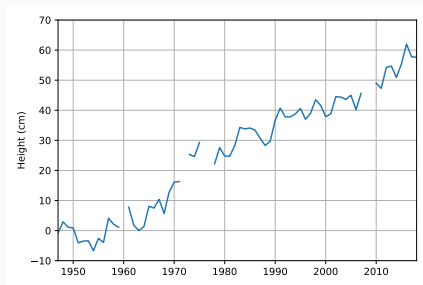
# Tide gauges are on land, and thus move with the land

Tide gauges measure sea level relative to land. If land moves, it will be recorded as a sea-level change!

- Subsidence and earthquakes can dominate the observed signal
- Local effects from ice sheets and GIA (other lectures!)

**Be sure that you isolate the process you're looking for!**

Subsidence in Grand Isle, near New Orleans



Source: PSMSL

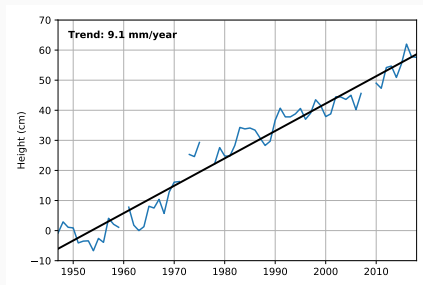
## Tide gauges are on land, and thus move with the land

Tide gauges measure sea level relative to land. If land moves, it will be recorded as a sea-level change!

- Subsidence and earthquakes can dominate the observed signal
- Local effects from ice sheets and GIA (other lectures!)

**Be sure that you isolate the process you're looking for!**

Example: subsidence in Grand Isle, near New Orleans



Source: PSMSL

# Relative and geocentric sea level

We call sea-level changes relative to the land *Relative Sea Level* (RSL) changes

- Tide gauges tell you RSL changes

We call sea-level changes relative to the center of the Earth *Geocentric Sea Level* (GSL) changes

- Satellite altimeters tell you GSL changes

The difference between both is *Vertical Land Motion* (VLM)

$$\text{GSL} = \text{RSL} + \text{VLM}$$



IJmuiden TG with GPS to measure VLM

# Datum control

Tide gauges measure sea level relative to some benchmark.

- We call this benchmark the 'datum'.
- Some countries use their national datum system to refer sea level (NAP in the Netherlands, Normal Null in Germany, and many others)
- Often, datum differs from tide gauge to tide gauge
- Relevant for mean sea level, but less so for sea-level changes.

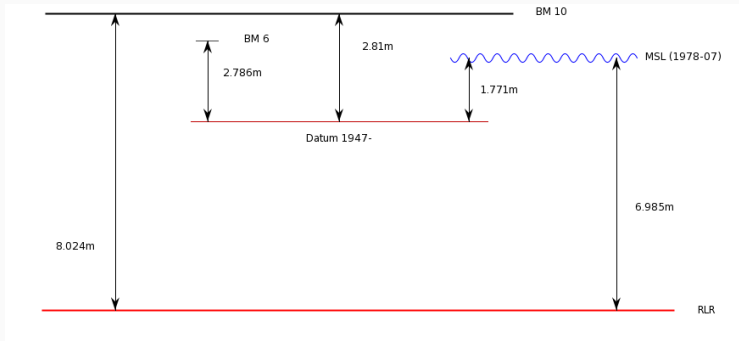
**Be aware of the datum when comparing two records!**



# Datum control

One important task of PSMSL: datum control.

- Level subsiding and replaced tide gauges to stable benchmarks
- RLR diagrams
- Ensures that you're looking at sea-level change



**Bottom line: always use Revised Local Reference (RLR) data and read the documentation!**

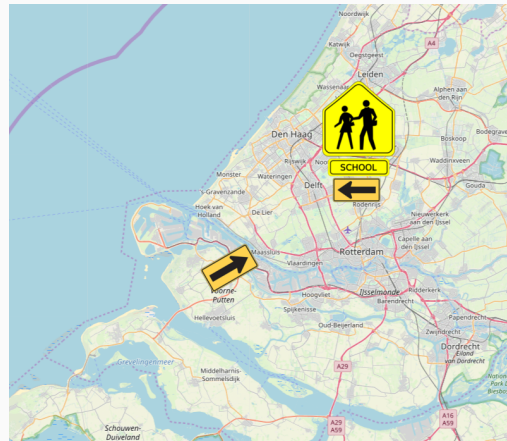
What signals can I expect in a  
tide-gauge record?

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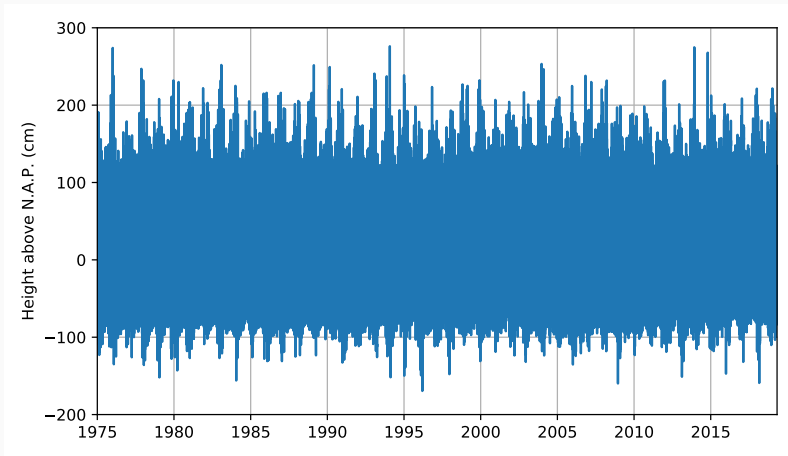
# Let's have a look at some real data!

The tide gauge in Maassluis is the nearest tide gauge station from this lecture hall that has a long and high-frequency record available.

- Hourly data since 1970
- Monthly and annual sea-level data from 1848



# High-frequency observations

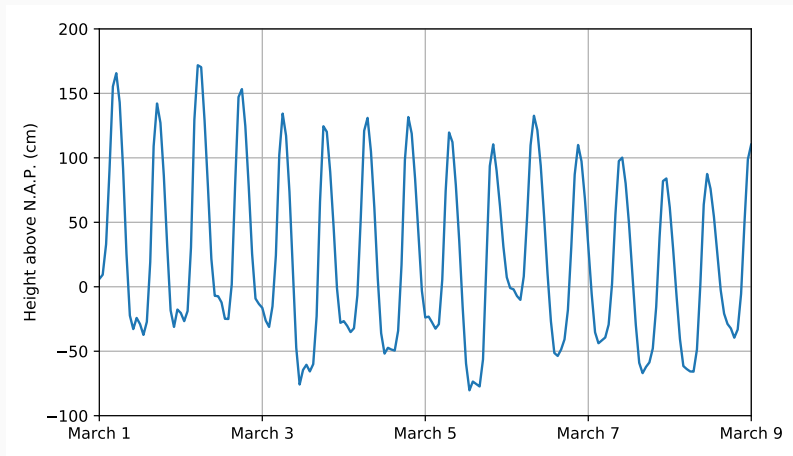


Data source: Rijkswaterstaat



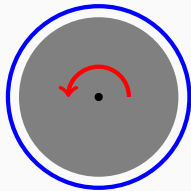
## Let's zoom in a little bit (Spring 2017)

Tides form the largest signal.



# A crash course in tides: the tidal potential

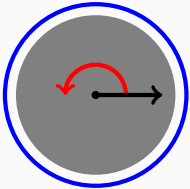
Tidal equilibrium



# A crash course in tides: the tidal potential

Tidal equilibrium

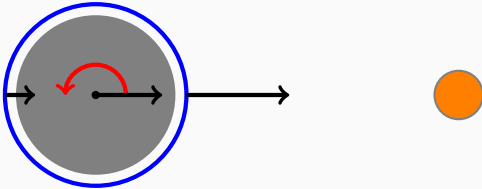
- Moon attracts water



# A crash course in tides: the tidal potential

## Tidal equilibrium

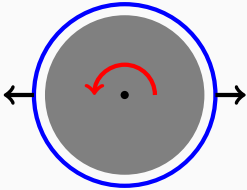
- Moon attracts water
- Ocean near moon more attracted than far side



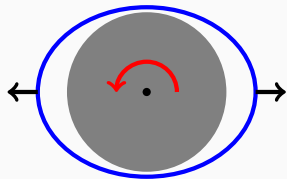
# A crash course in tides: the tidal potential

## Tidal equilibrium

- Moon attracts water
- Ocean near moon more attracted than far side
- Potential when we remove the body force



# A crash course in tides: the tidal potential

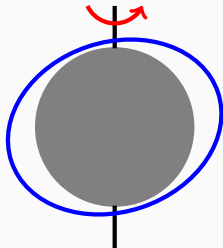


## Tidal equilibrium

- Moon attracts water
- Ocean near moon more attracted than far side
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- Two tidal bulges: semi-diurnal tide



# A crash course in tides: the tidal potential



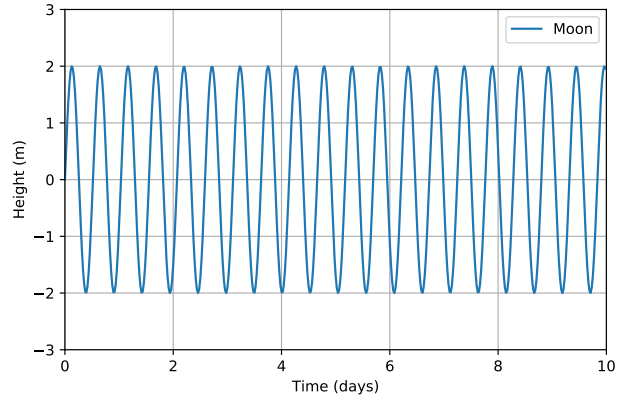
## Tidal equilibrium

- Moon attracts water
- Ocean near moon more attracted than far side
- Potential when we remove the body force
- Two tidal bulges: semi-diurnal tide
- Earth rotation axis is tilted, creating one larger and one smaller tide every cycle

# Sun and moon

The sun also causes a (smaller) tidal signal

- Mean lunar day: 24.85 hours

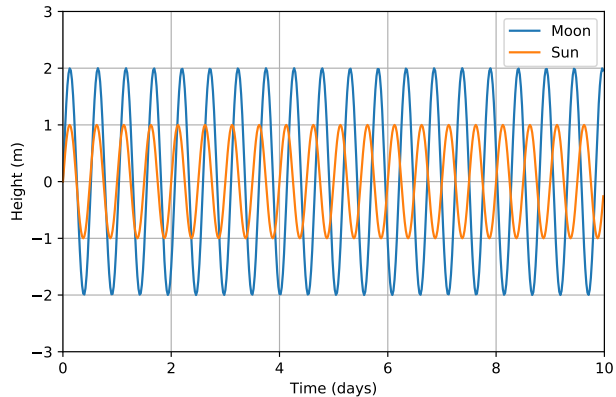




# Sun and moon

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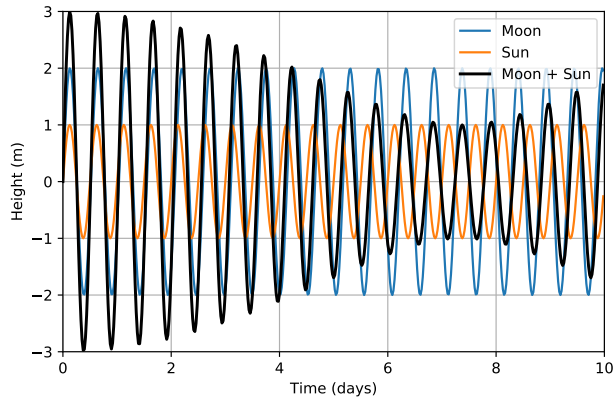
- Mean lunar day: 24.85 hours
- Mean solar day: 24 hours



# Sun and moon

The sun also causes a (smaller) tidal signal

- Mean lunar day: 24.85 hours
- Mean solar day: 24 hours
- Combination causes spring-neap cycle



# Equilibrium tides versus ocean tides

Ocean waves propagate too slow to adjust to tidal forcing:

- Real ocean tides deviate from tidal equilibrium
- On shallow-shelves, tides become very complicated

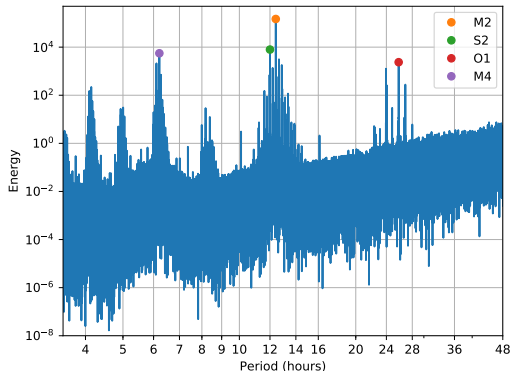
Bay of Fundy (East Canada) has a tidal range of 15 meter



Source: Wikimedia Commons

# Tidal constituents

## Periodogram of the Maassluis record

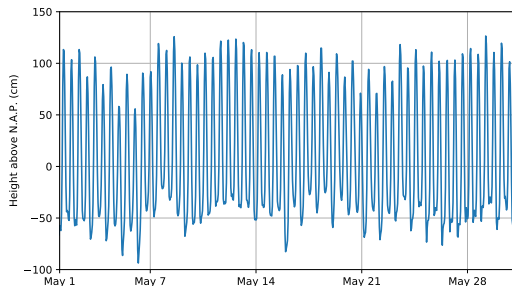


We can use a periodogram to estimate the tides:

- Peaks in the periodogram correspond to periodic signals. Higher peak: stronger cycle.
- We call these frequency peaks 'tidal constituents'
- We can spot the cycles due to the moon (M2) and the sun (S2)
- Tilt of the Earth axis: O1
- Many more tidal constituents!

# Estimating and predicting tides using least squares

Maassluis, May 2017

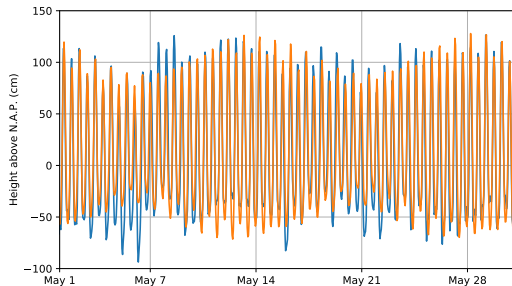


We can estimate the tidal signal using least squares:

- Estimate phase and amplitude of each constituent
- When we know them, we can also predict future tides
- Free Matlab/Python packages are available who do this for you! (UTide, t-tide, TASK)

# Estimating and predicting tides using least squares

Maassluis, May 2017



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## Coffee time



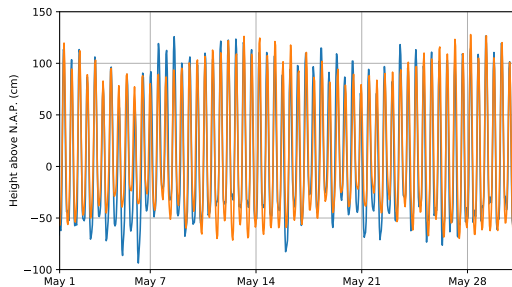
## Pressure, storms, and extremes

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# Pressure, storms, and extremes

Maassluis, May 2017



Tides only partially explain the day-to-day variations. How about wind?

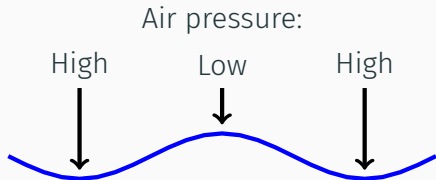
- Air pressure changes and wind affect sea level
- From the records, we can estimate expected storm-surge heights

# The inverted barometer effect

Air pressure pushes the ocean down.

High pressure: low sea level:

$$\Delta\eta = -\frac{1}{\rho g} (P_A - \overline{P_A})$$



$\Delta\eta$  Sea-level anomaly (m)

$\rho$  Water density ( $\text{kg}/\text{m}^3$ )

$g$  Gravitational acceleration ( $9.81 \text{ m}/\text{s}^2$ )

$P_A$  Local pressure (Pa)

$\overline{P_A}$  Mean pressure over ocean (Pa)

Works well for open ocean, but less effective along coasts.

# The December 5, 2013 storm



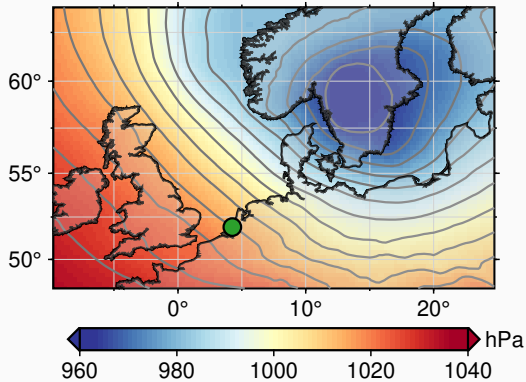
Flooding in Dagebull, Germany



Water reaches homes in Boston, UK

Photo credits: PRI, Peter Macdiarmid, Carsten Rehder

# The December 5, 2013 storm

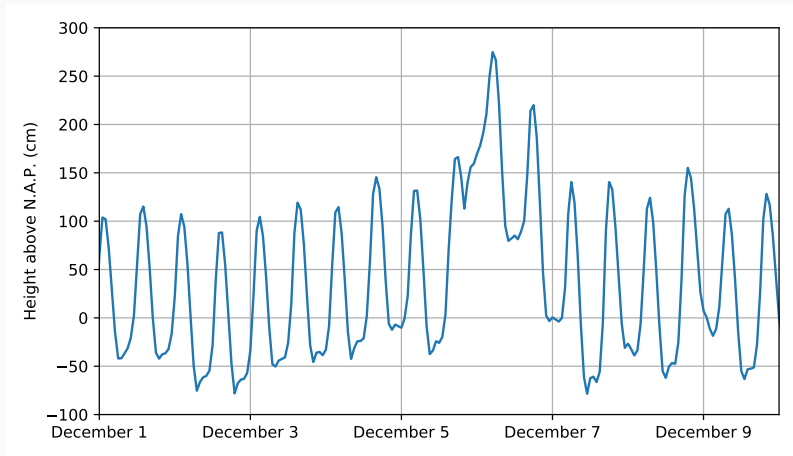


Source: ECMWF ERA5

The weather chart:

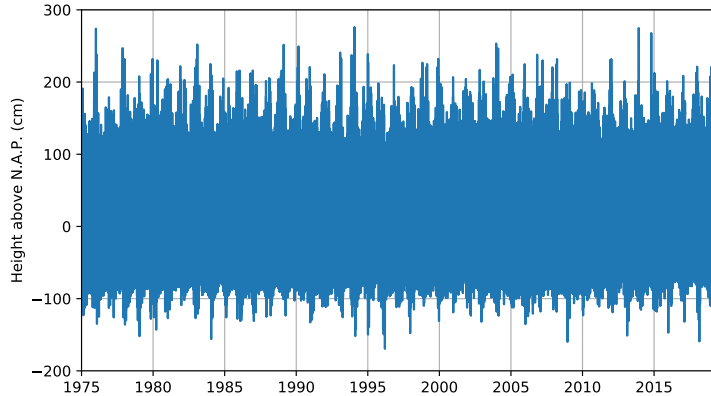
- Wind blows perpendicular to pressure gradient
- Isobars close to each other: strong wind
- Due to this storm, water piles up at the coast

## How does that look in our tide-gauge record?



Data source: Rijkswaterstaat

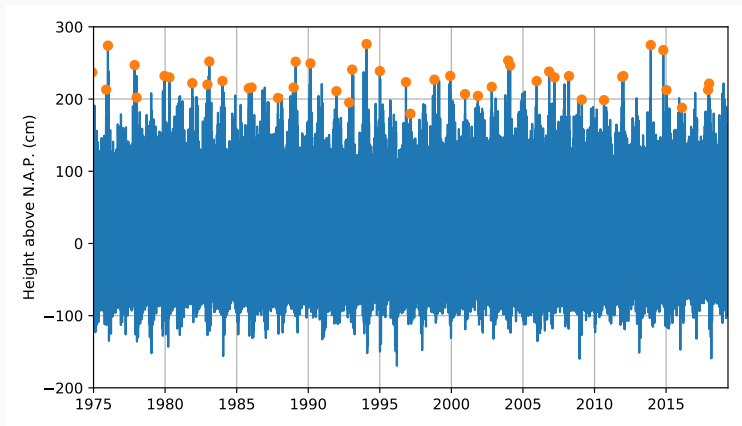
# Analysing storm surge characteristics



Source: Rijkswaterstaat

Can we estimate how often a specific surge will return? Yes, we can, using extreme-value statistics

# Analysing storm surge characteristics

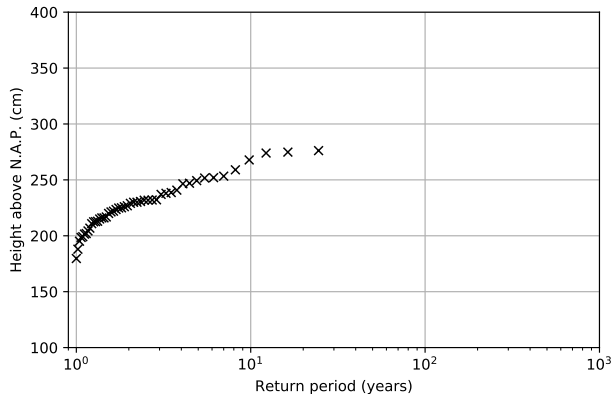


Source: Rijkswaterstaat

Can we estimate how often a specific surge will return? Yes, we can, using extreme-value statistics

- First select extreme events
- In this case, each annual maximum

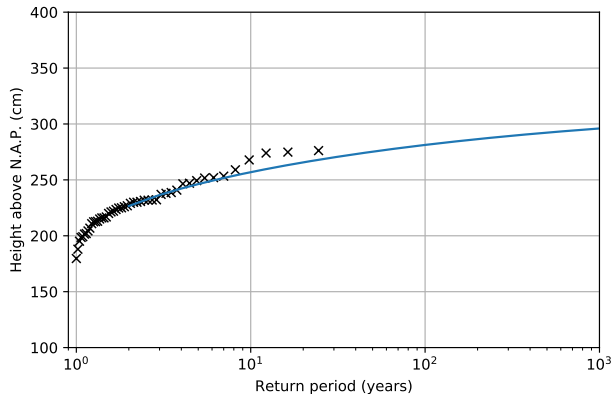
# Extreme-value analysis



We can estimate an extreme-value distribution from the maxima



# Extreme-value analysis



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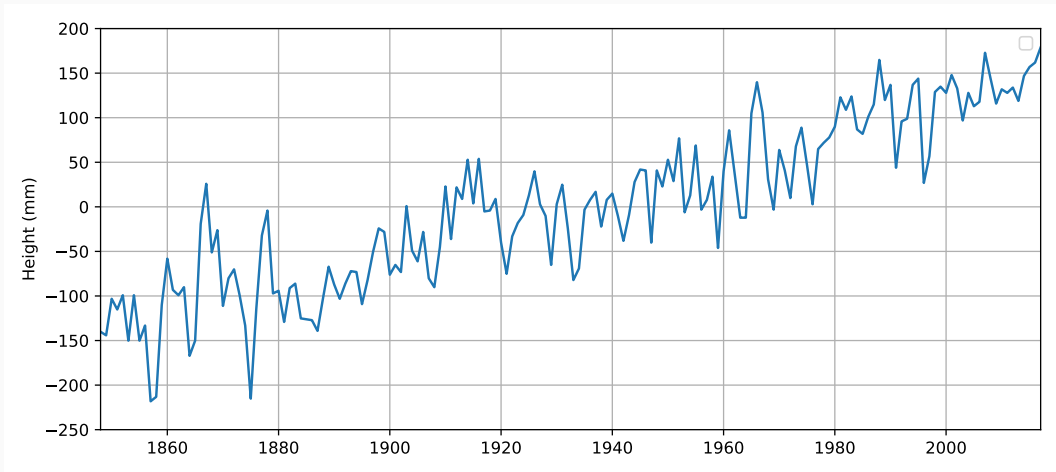
- Extreme-value return curve
- Expect a 1000-year event of  $\sim 300$  cm above NAP

## Long-term sea-level changes

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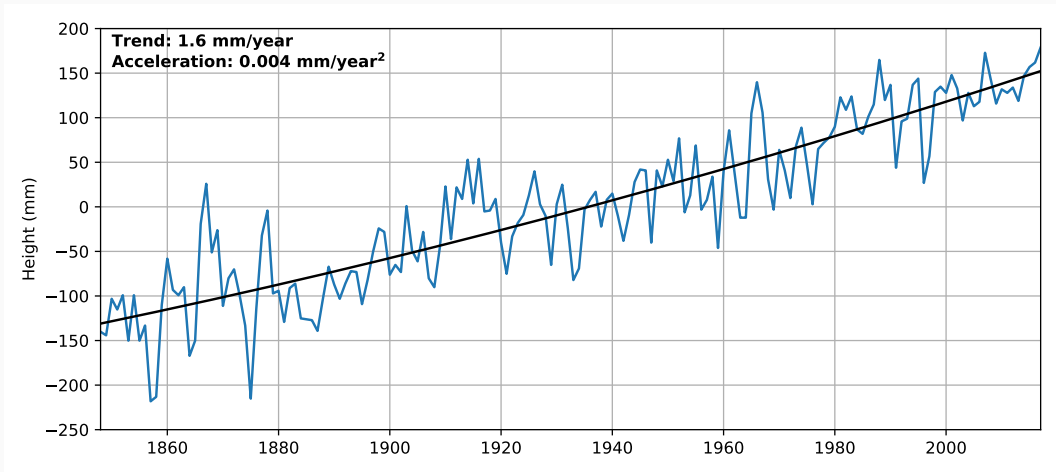
# Long-term sea-level changes in Maassluis

Continuous measurements since 1848



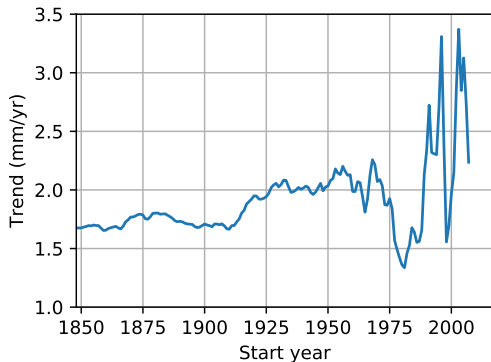
# Long-term sea-level changes in Maassluis

Continuous measurements since 1848



# A caveat on trends and accelerations

Trends and accelerations are always computed over a specific period



Always ask about the start and end points when confronted with trends and accelerations!

## Estimating global-mean sea-level changes from tide-gauge records

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# Estimating global sea-level changes from tide-gauge records

The main question:

How did global and regional sea level change over the last century?

To answer this, we have to average the sparse tide-gauge observations.

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This is challenging because:

- Incomplete records with a lot of data gaps



# Estimating global sea-level changes from tide-gauge records

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This is challenging because:

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- No even distribution over the oceans

# Estimating global sea-level changes from tide-gauge records

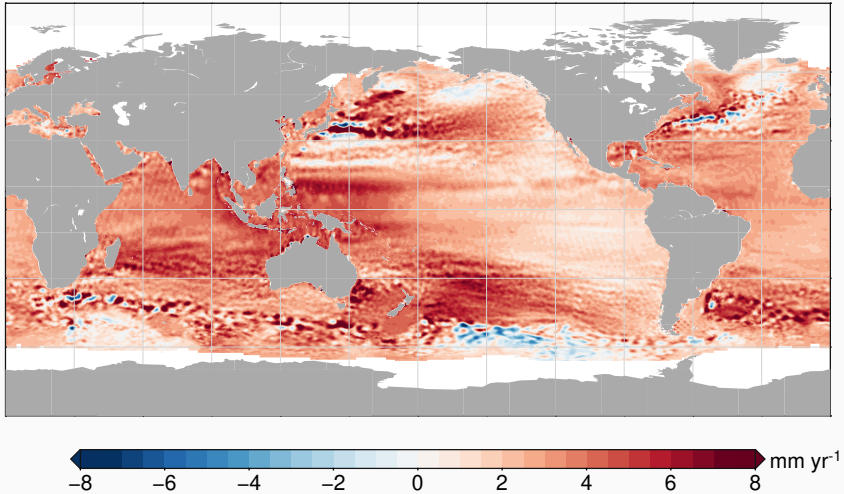
The main question:

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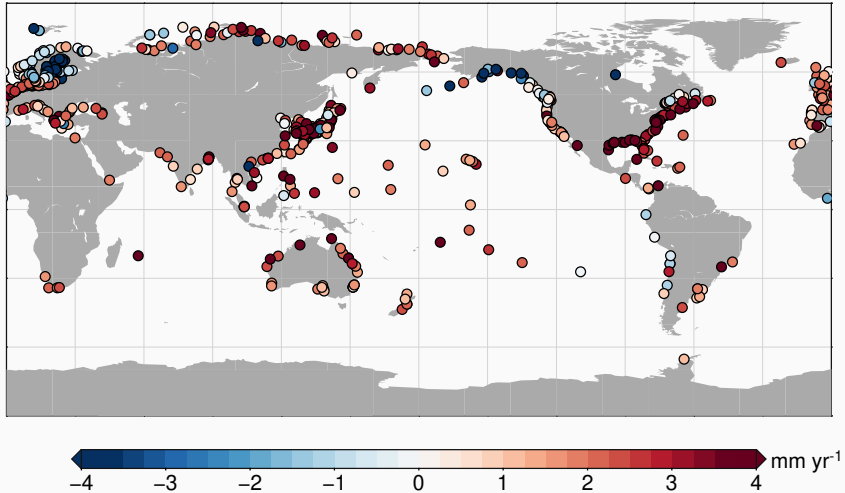
To answer this, we have to average the sparse tide-gauge observations.  
This is challenging because:

- Incomplete records with a lot of data gaps
- No even distribution over the oceans
- No single physical process causes a globally-uniform sea-level rise.

## Spatial variability in sea-level trends



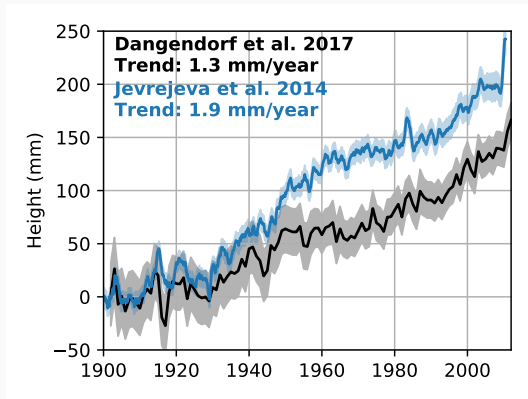
# Spatial variability in sea-level trends



# Virtual station method

Straightforward way to average multiple records:

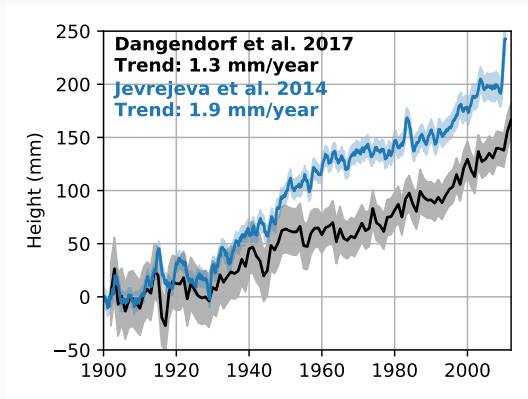
- Separate the global ocean into coherent regions
- Average two stations closest to each other into new 'virtual station' halfway
- Repeat until you only have a single station
- Last station is your regional curve
- Average regions to get global curve



# Virtual station method

Method is straightforward and easy to implement. However:

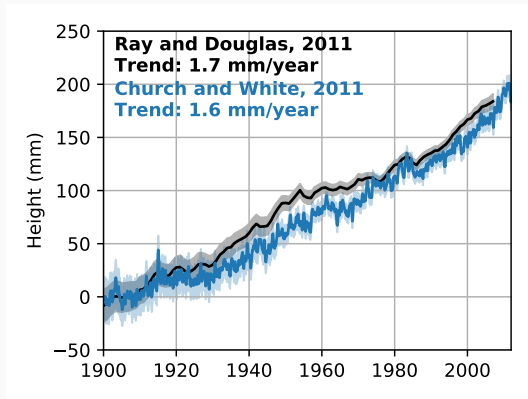
- Remote stations sometimes get very large weight
- Averaging stations is not trivial because they do not have common datum
- Difference in averaging causes largest difference between J14 and D17



# Empirical Orthogonal Functions

Use spatial patterns from satellite altimetry to estimate tide-gauge weight

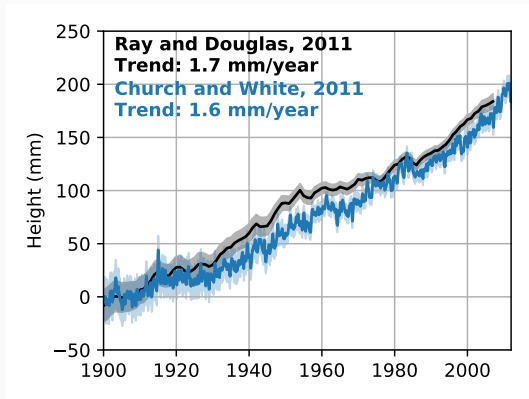
- Compute spatially coherent patterns in altimetry (EOFs)
- Estimate which tide gauges are representative for each pattern
- Extrapolate patterns back in time using these tide gauges
- This gives a spatio-temporal reconstruction, including GMSL



# Empirical Orthogonal Functions

Much more realistic weighting of stations, but:

- Are altimetry patterns representative for whole century?
- Altimetry does not work well along coasts, where tide gauges are located
- There are problems when estimating the global mean curve from the EOFs (See Calafat et al. 2013).

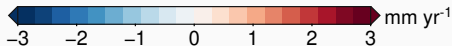
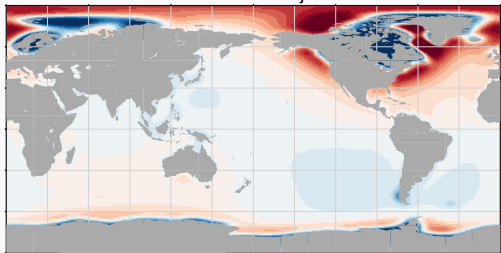




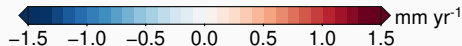
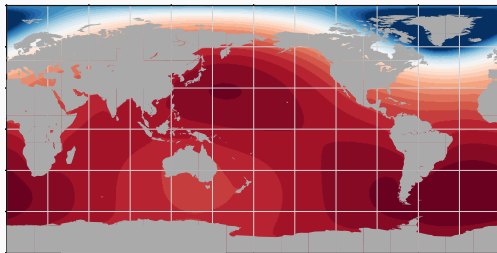
# Towards including prior knowledge to the system

We know that many physical processes have distinct spatial fingerprints

Glacial Isostatic Adjustment



Greenland Ice Sheet



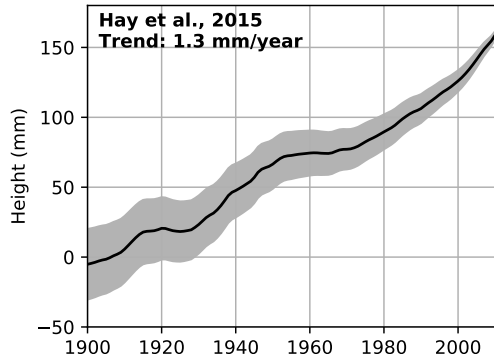
Source: GIA: Caron et al., 2018

Can we include them into the reconstructions?

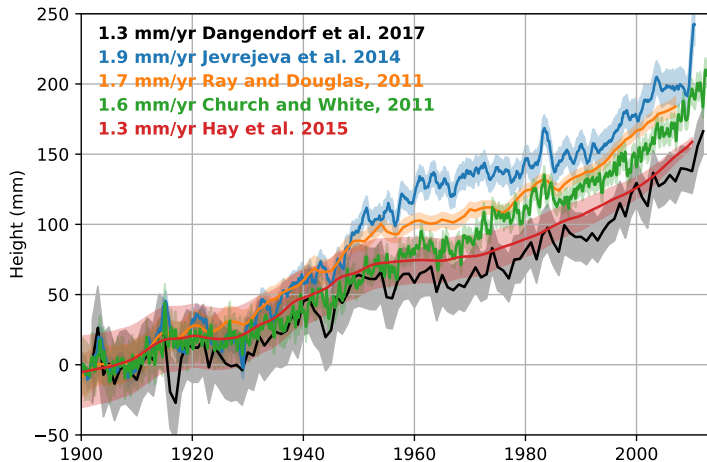
## Towards including prior knowledge to the system: Hay et al. 2015

An alternative approach by Hay et al., 2015: estimate the individual contributors to sea-level rise (ice/expansion etc) directly from tide-gauge data

- Determine spatial patterns of these contributors
- Build a statistical framework to estimate the contributors

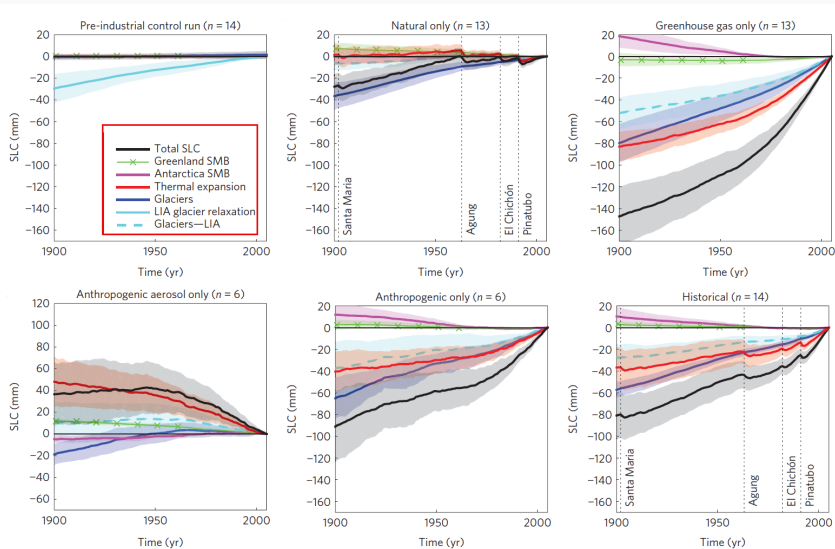


# Global reconstructions are not in agreement with each other



- Trends and variability differ between reconstructions.
- Reconstructions all show multi-decadal variability
- All agree with altimetry era
- All have positive acceleration

# Do we see a climate-change signal in sea-level records?



Source: Slangen et al., 2017, NGeo

## Summary

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- Measure storm surges and predict return periods
- Estimate long-term sea-level changes
- Reconstruct global sea level
- And there's much more!

## Summary

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Keep a few things in mind:

- Tide gauges observe a multitude of processes
- Know what a tide gauge does and does not measure
- Isolate the signal you want to know
- Keep an eye on datums and benchmarks
- Tide gauges measure relative sea level